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# **Research Article**



# A STUDY ON THE CRITICAL ADSORPTION DEPTH OF HIGH-RANK COAL

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## ABSTRACT

This paper presents the theoretical significance of the temperature-pressure-adsorption equation (TPAE) over the limitations of the Langmuir isothermal adsorption equation. The series isothermal adsorption data of high-rank coal from Chengzhuang coal mine in Shanxi Province, China were used to verify the practicality of the TPAE, and four parameters were obtained. According6.15% and sought, the adsorption value of any tests between 30°C-70°C and pressure between 0-20 MPa can be arbitrarily calculated, with an average relative error of less than 6.15%, and expressed by a three-dimensional adsorption surface. According to the total differential of the multivariate function is the sum of the differentials of each independent variable, assuming that the ground temperature gradient of Chengzhuang coal mine is 3°C/100 m and the ground pressure gradient is 1.0 MPa/100 m, it can be precisely calculated that both partial deviations of temperature and pressure. It can be approximately calculated that the critical adsorption depth of the low-rank coal is about 3200 m underground, the critical adsorption pressure is about 32 MPa, the critical adsorption temperature is about 114°C, and the critical adsorption capacity is 32.6 cm3/g.

Keywords: temperature-pressure-adsorption equation; Langmuir isothermal adsorption equation; partial deviations of temperature; partial deviations of pressure; the critical burial depth.

# INTRODUCTION

Coal bed gas is usually defined as a hydrocarbon gas absorbed mainly on the surface of coal matrix particles, free in coal pores or dissolved in coal seam water. The adsorption amount of gas on solid is a function of both temperature and pressure[1-4].At constant pressure, the curve which describes the relationship between adsorption amount and equilibrium temperature, is called isobaric adsorption. At constant adsorption amount, the curve which describes the relationship between adsorption pressure and equilibrium temperature, is called isosteric adsorption. At constant temperature, the curve which describes the relationship between adsorption amount and equilibrium pressure, is called isothermal adsorption. The Langmuir isothermal adsorption equation is the most famous equation to treat the data between adsorption amount and equilibrium pressure [5-8].All those three "iso adsorption" have transformed the three variables adsorption into two variables adsorption by fixing one variable. This kind of operation can make the understanding of the relationship between two variables easy, but not complete. Therefore, Langmuir parameters of a serials isothermal adsorptions at different temperatures cannot be used to mathematically explain why the absorption capacity of coal decreases with the increase of temperature, and its 'relationship regarding the phenomenon of with the increase of the buried depth, the adsorption capacity of coal bed methane gradually increases until it reaches a critical depth, and then decreases with the further increase of the buried depth. This paper will try to use a TPAE to overcome the limitation of Langmuir isothermal adsorption equation, and mathematically explain why the absorption capacity of coal decreases with the increase of temperature, why the adsorption gas content has a maximum value and what are the necessary and sufficient conditions for the adsorption gas content to appear at a maximum value.

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# DATA AND TEMPERATURE-PRESSURE-ADSORPTION EQUATION

# Sample

A low-rank coal from Chengzhuang(CZ) coal mine in Shanxi Province, China is used to verify the practicality of the TPAE, and its' mathematical derivations. The data and parameters of CZ coal samples are listed in Table 1.

Table1: The data and parameters of CZ coal sample [1]

parameter	data
R <sub>0, max</sub> /%	2.87
Vitrinite/%	62.6
Inertinite/%	23.3
Exinite/%	6.1
Mineral/%	8.19
Ash/%	14.8
Moisture/%	4.2

## The Langmuir adsorption equation

The Langmuir adsorption equation can be represented as:

$$V = \frac{abP}{1+bP} \tag{1}$$

here

a is the Langmuir volume.

b is the reciprocal of the Langmuir pressure.

The CZcoal under different testing temperatures is listed in Table 2. The temperature range is 30~ $70^{\circ}$ C and pressure is 0~20 MPa.

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 Table2: The Langmuir volume and the reciprocal of Langmuir pressure of CZ coal [1]

Experimental temperature/	a/cm <sup>3</sup> g <sup>-1</sup>	b/MPa <sup>-1</sup>
30	46.95	0.2267
50	45.45	0.1901
70	48.54	0.1019

Mathematically, the Langmuir equation only deals with a function between adsorption amounts and pressures under isothermal condition, therefore, it is not a function of the temperature.

### Temperature-pressure-absorbing equation (TPAE) [9-14]

Using the temperature and pressure as independent variables and adsorption amount as dependent variable, the TPAEcan be expressed as

$$V = \frac{1}{\sqrt{MT}} \left[ A + BP^{\beta} T^{1.5} \exp(\frac{\Delta}{T}) \right]$$
(2)

here:

- A is a constant of micro porous geometric shape for a fixed porous medium, dimensionless.
- B is the adsorption flow coefficient, which is related to the adsorption area, dimensionless.
- M is a molecular weight, and the molecular weight of methane is 16.
- P is pressure (MPa).
- T is the absolute temperature (K).
- V is the adsorption amount (cm<sup>3</sup>/g).
- β is a parameter which measures the relative influence of adsorption pressure, dimensionless.
- ∆ is the energy difference between the lowest potential energy and the activation energy of an adsorbed molecule in the adsorbed mass flow, which mainly measures the relative influence of the adsorption temperature, K.

The details regarding the regression of TPAE from series Langmuir adsorption has been presented early [9].

#### Verification

It is very necessary to verify the suitability of TPAE by comparing the adsorption amount of TPAE V<sub>TP</sub> and that of the Langmuir equation V<sub>LA</sub> under the exact same temperature and pressure. The relative error is defined as:

$$\delta_i = \frac{|V_{TP} - V_{LA}|}{V_{LA}} x100\%$$
(3-1)

The average relative error is defined as:

$$\overline{\delta} = \frac{1}{n} \sum_{i=1}^{n} \frac{|V_{TP} - V_{LA}|}{V_{LA}} x 100\%$$
(3-2)

here:

n is the total numbers of testing at different temperatures and pressures. There are 3Langmuir's temperatures, and for each temperature, 10 pressure values are chosen, from 1 to 20 MPa with a fixed interval of 2.0 MPa. The n is equal to 30.

 $V_{TP}$  is the calculated adsorption amount of TPAE at i conditions(temperature and pressure).

V<sub>LA</sub> is the calculated adsorption amount of Langmuir at i conditions(temperature and pressure).

# Partial differential equations of TPAE

As the influence of pore geometry constant, A is directly related to Knudsn diffusion, and is rather small comparing to rest part of TPAE. Therefore, the TPAE can be simplified as

$$V = \frac{B}{\sqrt{M}} T exp\left(\frac{\Delta}{T}\right) P^{\beta} \tag{4}$$

The equation (4) indicates that the adsorption amount still is a function of both temperature and pressure. For a trinary equation, its total differential of adsorption amount should be presented as the sum of the differentials of each independent variable, temperature, and pressure:

$$dV = \left[\frac{\partial V}{\partial T}\right]_P dT + \left[\frac{\partial V}{\partial P}\right]_T dP$$
(5)

here:

 $\left(\frac{\partial V}{\partial P}\right)_T$  is the partial differential with respect to pressure under isothermal condition, and  $\left(\frac{\partial V}{\partial T}\right)_P$  is the partial differential with respect totemperatureunder the isobaric condition.

The partial differential equation of temperature is.

$$\left(\frac{\partial V}{\partial T}\right)_{P} = \frac{B}{\sqrt{M}} P^{\beta} exp\left(\frac{\Delta}{T}\right) \left(1 - \frac{\Delta}{T}\right)$$
(6)

According to the equation (6), under the isobaric condition,  $\left(\frac{\partial V}{\partial T}\right)_p$  could be either negative or positive. If  $\frac{\Lambda}{T}$  is larger than 1,  $\left(\frac{\partial V}{\partial T}\right)_p$  is negative, less than zero. Then the right-hand side of equation (6) must be less than zero, which means that increasing temperature has negative effect. If  $\frac{\Lambda}{T}$  is smaller than 1,  $\left(\frac{\partial V}{\partial T}\right)_p$  is positive, larger than zero, which means that increasing temperature has negative effect. If  $\frac{\Lambda}{T}$  is smaller than 1,  $\left(\frac{\partial V}{\partial T}\right)_p$  is positive, larger than zero, which means that increasing temperature has a positive effect. Therefore, equation (6) illustrates that, for most coal samples' isothermal adsorptions, as  $\Lambda$  larger than T, the adsorption volume will decrease with temperature increasing. Even under isobaric condition, according to the equation (6), both pressure "P" and parameter " $\beta$ " have contributed to the value of the partial differential with respect to T.

The partial differential equation of pressure is

$$\left(\frac{\partial V}{\partial P}\right)_{T} = \frac{B}{\sqrt{M}} T \exp\left(\frac{\Delta}{T}\right) \beta P^{\beta - 1} \tag{7}$$

Under isothermal condition, because all parameters, B, M, T, P and  $\beta$  are positive, never being negative by any chance, the right side of equation (7) is always positive. Therefore, the adsorption pressure always has a positive influence, which has been approved by all isothermal adsorptions. Even under isothermal condition, both temperature "T" and parameter " $\Delta$ " have contributed into the value of the right-hand side of equation (7).

From Equations (5), (6), and (7), The total differential and partial differentials can be calculated if the following equations being used in the calculation:

$$T = \frac{T_1 + T_2}{2} \tag{8-1}$$

$$P = \frac{P_1 + P_2}{2} \tag{8-2}$$

$$dT = T_2 - T_1 (9-1)$$

$$dP = P_2 - P_1 \tag{9-2}$$

$$V_i = V_{i-1} + dV_i$$
 (10)

Based on the coal samples isothermal adsorption temperature and pressure range, both increase integral of temperature and pressure are designed.

# **RESULTS AND DISCUSSIONS**

# TPAE

The four parameters of TPAE regressed from Table 2 parameters of CZ coal are listed in Table 3.

 Table 3: The TPAE parameters retrieved from isothermal adsorption measurements of CZcoal.

Parameter	value	
А	0.168	
В	0.003583	
$\Delta/K$	1112	
β	0.4789	
$ar{\delta}$ /%	6.15	

The final average relative error of low-rank coal is 6.15%. It is reasonable to conclude that TPAE treats accurately a series of isothermal adsorption. Since the TPAE is a mathematical expression of temperature-pressure-adsorption, it could be presented in a threedimensional picture as shown in Figure 1. The 3 rows' points are corresponding 3 Langmuir's temperatures.

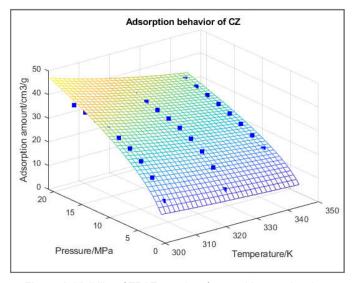


Figure 1: Visibility of TPAE cured surface and Langmuir points.

From Figure 1, the3 rows' Langmuir points are agreed with the TPAE cured surface. This approves that TPAE treats accurately a series of isothermal adsorption.

### Partial differentials

The results of total differential and partial differentials are listed in Table 4. There are three phenomena that should be noticed.

T1/K T2/K P1 P2 ðV ⁄ ðV dT dP dV v **OT** \<u></u> *∂P* 291 294 2 -0.1365 4.54864 3 4.139 16 1 1 294 297 2 3 -0.1654 3.38802 3 2.892 18.9 1 297 300 3 4 -0.1845 2.76542 21.2 3 2,212 1 300 303 4 5 -0.1978 2.36119 3 1.768 22.9 1 303 306 5 6 -0.2072 2.07126 3 1 1.45 24 4 306 309 6 7 -0.2137 1.85018 3 1.209 1 25.6 312 7 8 -0.218 309 1.67444 3 1 1.02 26.6 9 -0.2207 312 315 8 1.53051 3 1 0.868 27.5 315 318 9 10 -0.2221 1.40994 3 1 0.744 28.2 318 321 10 11 -0.2225 1.30713 3 1 0.64 28.9 321 324 12 -0.2221 1.21823 3 0.552 29.4 11 1 324 -0.221 327 12 13 1.14046 3 1 0.478 29.9 327 330 13 14 -0.2194 1.07176 3 0.414 30.3 1 330 333 14 15 -0.2173 1.01058 3 0.359 30.7 1 333 336 15 16 -0.2149 0.9557 3 1 0.311 31 336 339 16 17 -0.2123 0.90619 3 0.269 31.2 1 -0.2094 0.233 339 342 17 18 0.86127 3 1 31.5 345 -0.2064 0.82032 0.201 31.7 342 18 19 3 1 345 348 19 20 -0.2032 0.78284 3 1 0.173 31.8 348 351 20 21 -0.2 0.74841 3 1 0.148 32 351 354 21 22 -0.1967 0.71666 3 1 0.127 32.1 354 357 22 23 -0.1933 0.68729 3 1 0.107 32.2 357 360 23 24 -0.1899 0.66006 3 1 0.09 32.3 25 3 360 363 24 -0.1865 0.63473 1 0.075 32.4 363 366 25 26 -0.1831 0.61113 3 0.062 32.5 1 366 369 26 27 -0.1797 0.58907 3 1 0.05 32.5 369 372 27 28 -0.1763 3 0.039 32.5 0.56843 1 375 372 28 29 -0.173 0.54907 3 0.03 32.6 1 375 378 29 30 -0.1697 0.53088 3 0.022 32.6 1 378 381 30 31 -0.1664 0.51376 3 0.015 32.6 1 -0.1632 381 384 31 32 0.49762 3 1 0.008 32.6 384 387 32 33 -0.16 0.48238 3 1 0.002 32.6 387 390 33 34 -0.1569 0.46798 3 1 -0 32.6 390 393 34 35 -0.1539 0.45434 3 1 -0.01 32.6 393 396 35 36 -0.1509 0.44142 3 1 -0.01 32.6

### V=11.9cm<sup>3</sup>g<sup>-1</sup>at 291K and 1 MPa.

First, under testing temperature range (18~120 $\Box$ , 291 ~393K), for CZ coal with  $\Delta$ =1112K, its partial differential of temperature should be always less than zero. This proves the observation of the adsorption volume decreases as the temperature increases.

Second, under testing pressure range (1~20 MPa), CZ coal's partial differential of pressure is always greater than zero. This proves the observation of the adsorption volume increase as the pressure increases.

Since the total differential of the multivariate function is the sum of the differentials of each independent variable, then a partial differential of temperature(being always less than zero)adds a partial differential of pressure(being always greater than zero)could produce a turning

 Table 4: The results of total differential and partial differentials of CZ coal under the tested temperature and pressure

point, at where the total differential of CZ is zero, along with the buried depth increasing.

The partial differential of both variables can be seen in Figure 2.

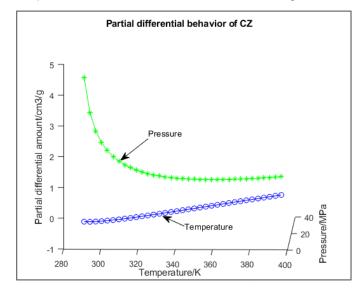


Figure 2: Partial differential of temperature and pressure

# **Buried depth**

When the buried depth of coal is increased, both temperature and pressure are increased. Therefore, the total differential of adsorption amount is positive, the adsorption amount is increased, as shown in Table 4, T < 387K, P<32MPa. When the buried depth of coal is increased, both temperature and pressure are increased, the total differential of adsorption amount is approaching zero, the adsorption amount is approaching zero, the adsorption amount is increased, both temperature and pressure are increased, the total differential of adsorption amount is approaching zero, the adsorption amount is approaching a maximum. After this critical depth, even if the buried depth of coal is increased, both temperature and pressure are increased, but the total differential of adsorption amount is negative, the adsorption amount is reducing as shown in Table 4, T > 390K, P > 33MPa.

Assuming the temperature of the constant temperature layer at CZ coal was 15°Cthe ground temperature gradient of 3°C /100m and the pressure gradient of 1MPa / 100m,the relationship between the buried depth and the adsorption amount of CZ coal is depictured in Figure 3.

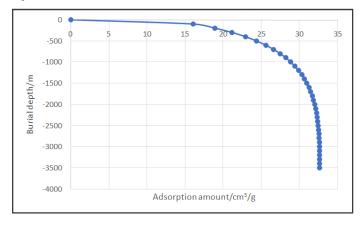


Figure 3: The relationship between the burial depth and the adsorption amount of CZ coal

Based on the assumption of the ground temperature gradient of  $3^{\circ}C/100m$  and the pressure gradient of 1MPa / 100m, the critical depthis predicted at the depth between 3200m and 3300m with a

maximum adsorption amount of 32.6 cm<sup>3</sup>/g. Before reaching the critical depth, the total differential of adsorption amount is positive, the adsorption amount is increased. After passing the critical depth, the total differential of adsorption amount is negative, the adsorption amount is reducing.

# CONCLUSIONS

The set of five temperatures' isothermal adsorption data of CZ coal of Shanxi, China have been used to regress and to calculate the parameters of TPAE. This operation has transformed the Langmuir equations into trinary (temperature-pressure-absorbing) equation with the average relative errors is 6.15%. The TPAE curvature surface and adsorption points match very well. Both numerical and graphical evidence approved that TPAE is applicable to interpreting the series isothermal adsorption data. TPAE is a trinary (temperature-pressure-absorbing) equation, its partial differential of temperature partial differential of pressure and total differential can be numerically calculated. All calculation results of the WT coal sample in the measured temperature range  $(30~70\Box)$  and pressure range (0~20 MPa) have been presented in a table format.

Under the isobaric condition, the partial differential with respect to T,  $\left(\frac{\partial V}{\partial T}\right)_P$ , is negative, so the adsorption amount is decreasing with increasing temperature. Under the isothermal condition, the partial differential with respect to P,  $\left(\frac{\partial V}{\partial P}\right)_T$ , is positive, so the adsorption amount is increasing with increasing pressure. If the ground temperature gradient of 3°C /100m and the pressure gradient of 1MPa / 100m, the critical depth is predicted at the depth between 3200m and 3300m with a maximum adsorption amount of 32.6 cm<sup>3</sup>/g.

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